

# A new interface between GAP and Singular: libsing

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# Overview

- 1 What is this all about?
- 2 A very short example
- 3 The gory details

# The protagonists

- “**GAP** is a system for computational discrete algebra, with particular emphasis on Computational Group Theory.
- “**Singular** is a computer algebra system for polynomial computations, with special emphasis on commutative and non-commutative algebra, algebraic geometry, and singularity theory. **Singular** provides highly efficient core algorithms, a multitude of advanced algorithms in the above fields, [...]”
- **libsing** provides an efficient bridge between these two systems.

## Related work

- [GAP](#) package “singular” by Marco Costantini and Willem de Graaf
  - Last regular update in 2006, based on Singular 2
  - Uses “screen scraping”  $\rightsquigarrow$  fragile; inefficient
  - No generic way to transfer complex data structures.
  - No easy access to complete functionality of [Singular](#).
- Packages “IO\_ForHomalg” & “RingsForHomalg by homalg project
  - Supports [Singular](#) 3 and 4
  - Based on IO package, but in the end also does “screen scraping”
  - Avoids data conversions where possible  $\rightsquigarrow$  efficient at what it does
  - Does not attempt to give access to complete functionality of [Singular](#) “out of the box”.
- [Sage](#) includes both [GAP](#) and [Singular](#), could be used as “interface”

# Features

- `libsing` is a `GAP` package, loaded by the `GAP` interpreter, but also links against `Singular` 4 (compiled as a shared library).
- `libsing` consists of a part written in C++, and a part written in the `GAP` programming language.
- `libsing` grants access to the complete functionality of `Singular` from the high-level `GAP` programming language. With it you may ...
  - ... access `Singular` objects via `GAP` wrapper objects;
  - ... convert between `Singular` and `GAP` objects;
  - ... access `Singular` C++ kernel functions;
  - ... use `Singular` interpreter intrinsics;
  - ... use `Singular` libraries;all from within `GAP`.

## Short example: Singular version

The following example is taken from the [Singular](#) manual, specifically from the entry for `stdfglm`, a library command for computing a Gröbner basis.

```
> ring r = 0, (x,y,z), lp;  
> ideal i = y3+x2, x2y+x2, x3-x2, z4-x2-y;  
> stdfglm(i);  
_[1]=z12  
_[2]=yz4-z8  
_[3]=y2+y-z8-z4  
_[4]=xy-xz4-y+z4  
_[5]=x2+y-z4
```

## Short example: Straight conversion to GAP

The following is a straight conversion to [GAP](#) code using the low-level access to [Singular](#) interpreter intrinsics and library functions.

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);  
<singular ring>  
gap> i := SI_ideal(r, "y3+x2,x2y+x2,x3-x2,z4-x2-y");  
<singular ideal (mutable), 4 gens of deg <= 4>  
gap> SIL_stdfglm(i);  
<singular ideal (mutable), 5 gens of deg <= 12>  
gap> Display(last);  
z12,  
yz4-z8,  
y2+y-z8-z4,  
xy-xz4-y+z4,  
x2+y-z4
```

## Short example: Better GAP version

Or we can do without those strings and use a more “GAP-style” way of entering the polynomials:

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);;
gap> AssignGeneratorVariables(r);
#I Assigned the global variables [ x, y, z ]
gap> i := SI_ideal([y^3 + x^2, x^2*y + x^2,
>                 x^3 - x^2, z^4 - x^2 - y]);
<singular ideal (mutable), 4 gens of deg <= 4>
gap> SIL_stdfglm(i);
gap> Display(last);
z12,
yz4-z8,
y2+y-z8-z4,
xy-xz4-y+z4,
x2+y-z4
```

# Troubled data exchange

- **GAP** and **Singular** deal with many similar kinds of data: machine integers, multiprecision integers, lists, matrices, polynomials, etc.
- ... but they represent them quite differently.
- They also use radically different memory management schemes:
- **GAP**: generational moving garbage collector
  - memory does not have to be explicitly released;
  - the exact location of an object in memory can change.
- **Singular**: traditional memory manager plus reference counting
  - memory must be freed explicitly;
  - objects live in a fixed position during their life time.
- Need to bridge these differences with as little overhead as possible.

# Wrapping objects

- **Singular** objects to be used from **GAP** are put into wrapper objects.
- **Singular** objects stay in a fixed place, the **GAP** wrapper may move.
- Benefit from the garbage collector housekeeping: if the wrapper is garbage collected, we free the wrapped object.
- **Singular** has a notion of an “active ring”, implicitly used for computations. **libsing** hides this concept from **GAP** and the user.

# Wrapping objects II

There are three kinds of wrappers, consisting of two or four machine words (32 or 64 bit), respectively. Namely for ...

ring free objects:

Attribute bits & type
C++ pointer to <b>Singular</b> object

ring dependant objects:

Attribute bits & type
C++ pointer to <b>Singular</b> object
<b>GAP</b> reference to wrapper for ring
C++ pointer to <b>Singular</b> ring

rings:

Attribute bits & type
C++ pointer to <b>Singular</b> object
<b>GAP</b> reference to wrapper for ring's zero
<b>GAP</b> reference to wrapper for ring's one

There can also be an additional word for the extended attributes.

# Converting data

- (Un)wrapping objects is fast, has low memory overhead.
- But sometimes one needs to convert data, e.g.: given some **GAP** data, convert it to **Singular**, perform heavy computations, convert the result back to **GAP**.
- Machine ints are converted directly.

```
gap> SI_int(3);  
3
```

- Multi precisions ints: **GAP** uses low-level, **Singular** high-level GMP interface  $\implies$  conversion is necessary, requires copying data.

```
gap> x := SI_bigint(3^20);  
<singular bigint:3486784401>  
gap> _SI_Intbigint(x);  
3486784401
```

## Converting data II

- Containers (intvecs, intmats, lists, etc.) are converted recursively.

```
gap> v := SI_intvec([1,2,3]);  
<singular intvec:[ 1, 2, 3 ]>  
gap> _SI_Plistintvec(v);  
[ 1, 2, 3 ]
```

- Rings, their elements, ideals, ..., are not (automatically) converted, (exception: rationals,  $\mathbb{Z}/p\mathbb{Z}$ )

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);  
<singular ring>
```

- Instead of converting e.g. polynomials, the goal is to implement high level [GAP](#) APIs for such objects (e.g. querying the degree, coefficients, etc.).

## Low level: Calling into the Singular kernel

- Wrappers for select C / C++ functions from the [Singular](#) kernel.
- For each supported function, we copy its declaration from the [Singular](#) kernel, augmenting it with some “hints”:

```
poly pp_Mult_nn(poly p, number n, const ring r);  
poly p_Mult_nn(DESTROYS poly p, number n, const ring r);
```

- When compiling [libsing](#) (via `make`), this is read by a code generator, which produces C wrappers accessible from [GAP](#):

```
_SI_pp_Mult_nn  
_SI_p_Mult_nn
```

- Right now only a small set of functions is mapped, but it is very easy to extend this.

## Middle level: Using interpreter intrinsics

- “Interpreter intrinsics”: functions provided by the [Singular](#) interpreter, but implemented in C++ (such as `betti`, `std`, `ncols`).
- Take different data types as input as the kernel functions.
- [Singular](#) interpreter contains a table describing all intrinsics (including names, parameter types; overloading possible)
- When compiling [libsing](#), this table is read and appropriate wrappers are created as [GAP](#) functions

```
BindGlobal("SI_degree",  
  function(a)  
    return _SI_CallFunc1(285,a);  
  end );
```

## Middle level: Using Singular libraries

- Functions and libraries written in the [Singular](#) language are usable.

```
gap> SIL_submat;  
Error, Variable: 'SIL_submat' must have a value  
not in any function at line 44 of *stdin*  
gap> SI_LIB("matrix.lib");  
gap> s := SI_ring(0,["a","b"]);;  
gap> m := SI_matrix(s,2,2,"a,b,ab,1");  
<singular matrix (mutable):  
a, b,  
ab,1 >  
gap> y := SIL_submat(m,SI_intvec([1,2]),SI_intvec([2]));  
<singular matrix (mutable):  
b,  
1 >
```

- Currently can not use [GAP](#) functions from [Singular](#).

## High level: Dressing it up as GAP objects

- Finally, we also intend to provide high-level GAP wrappers for Singular functionality.

- For example, operators like +, -, \* are overloaded.

```
gap> SI_bigint(3^25) + SI_bigint(7^36);  
<singular bigint:2651730845859653472626311991044>
```

- This is still a lot of work if one wants to cover everything.